



## ISR\*FSR Interference from $\mathcal{K}\mathcal{K}$ MC generator

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QUESTIONS:

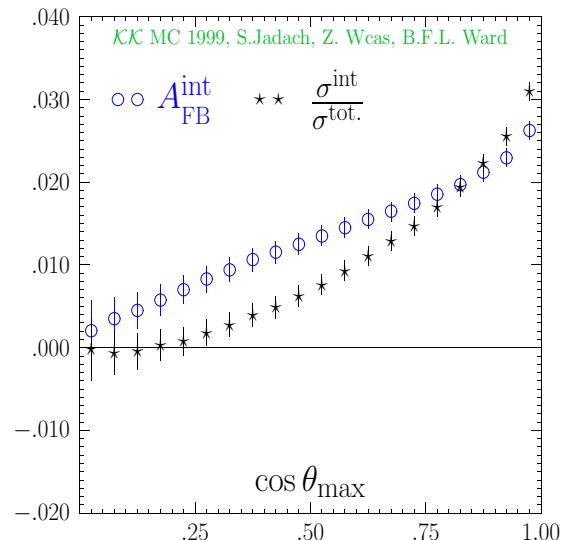
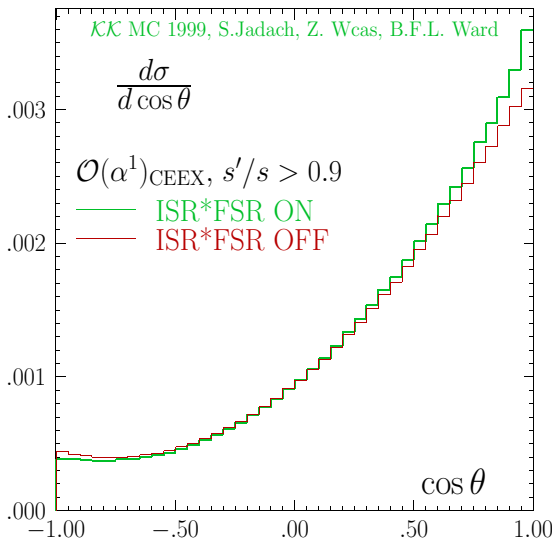
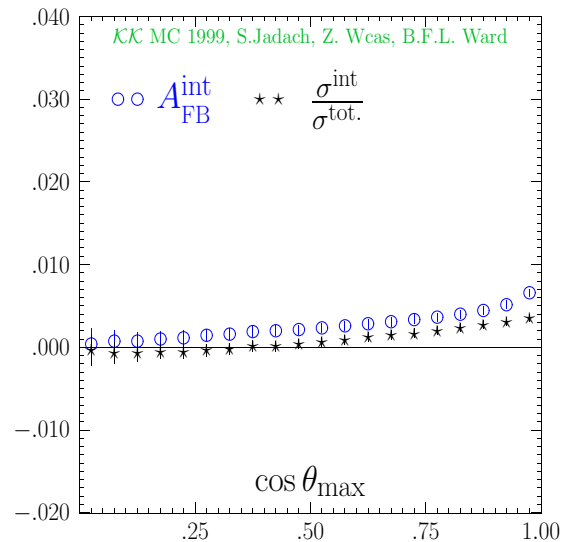
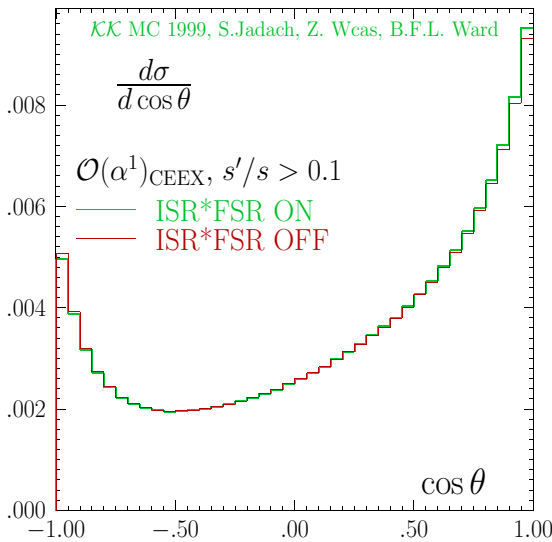
- How big is ISR\*FSR Interference in  $\sigma_{tot}$  and  $A_{FB}$ ?
- Do we know it at  $\mathcal{O}(\alpha^1)$ ?
- Do we know it beyond  $\mathcal{O}(\alpha^1)$ ?
- How sensitive it is to cut-off changes?
- Conclusions

For  $\mathcal{K}\mathcal{K}$  MC check <http://home.cern.ch/~jadach>

DESY

# ISR\*FSR interf. in angular distribution

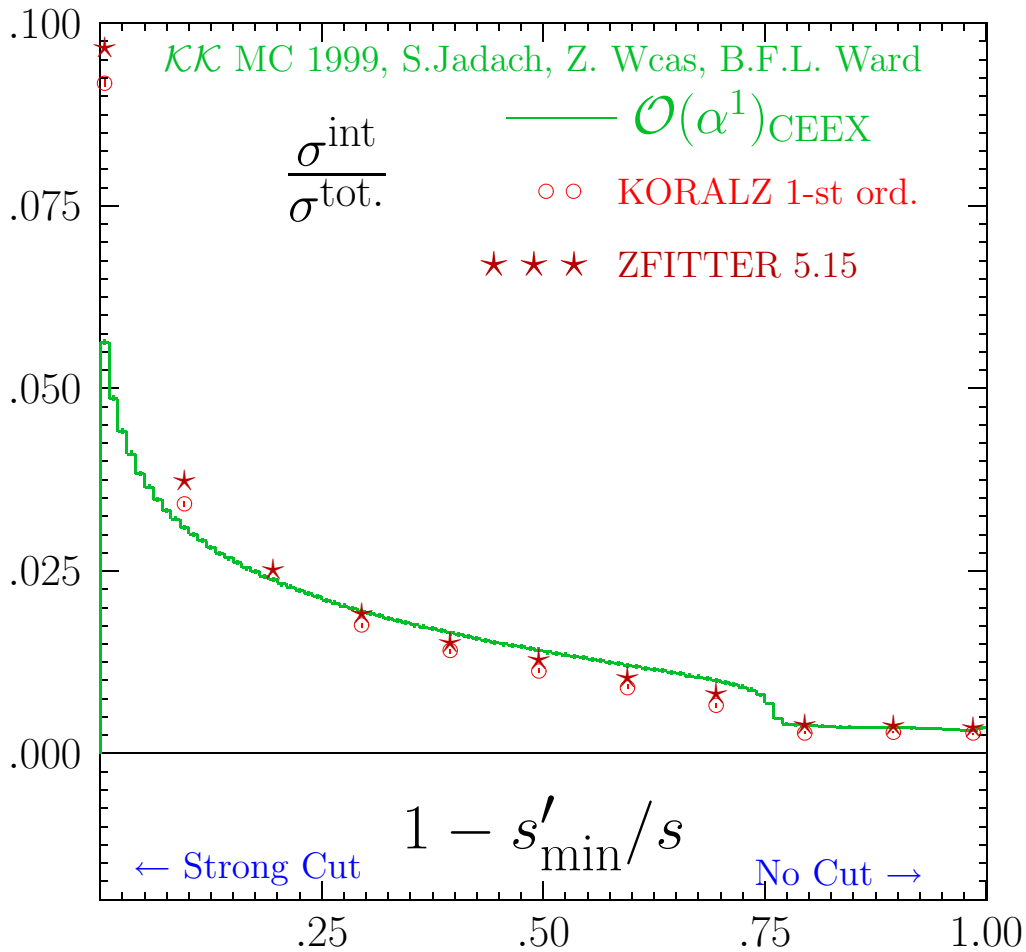
The influence of ISR\*FSR interference at 189GeV. The energy cut is on  $s'/s$ , where  $s' = m_f^2_{f\bar{f}}$ . The angular cut is  $|\cos\theta| < \cos\theta_{\max}$ . Scattering angle is  $\theta = \theta^\bullet$ . [Angle  $\theta^\bullet$  is defined in Phys. Rev. **D41**, 1425 (1990)]



DESY

## ISR\*FSR in $\sigma$ , cut-off dependence

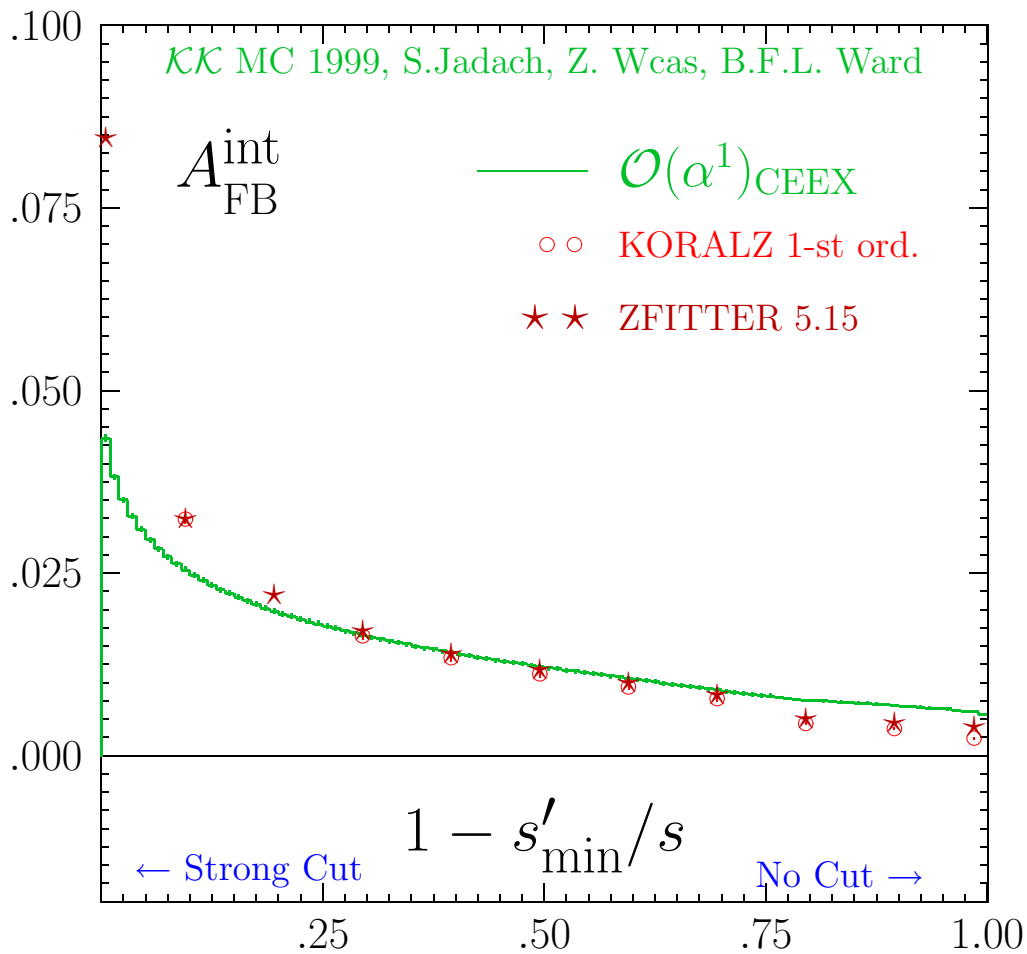
The ISR\*FSR interference correction to  $\sigma(s'_{\min})$  at 189GeV. No cut in  $\cos\theta^*$ . From  $\mathcal{K}\mathcal{K}$  M.C. with  $\mathcal{O}(\alpha^1)_{\text{CEEX}}$  exponentiation at the amplitude level.



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## ISR\*FSR in $A_{FB}$ , energy cut-off study

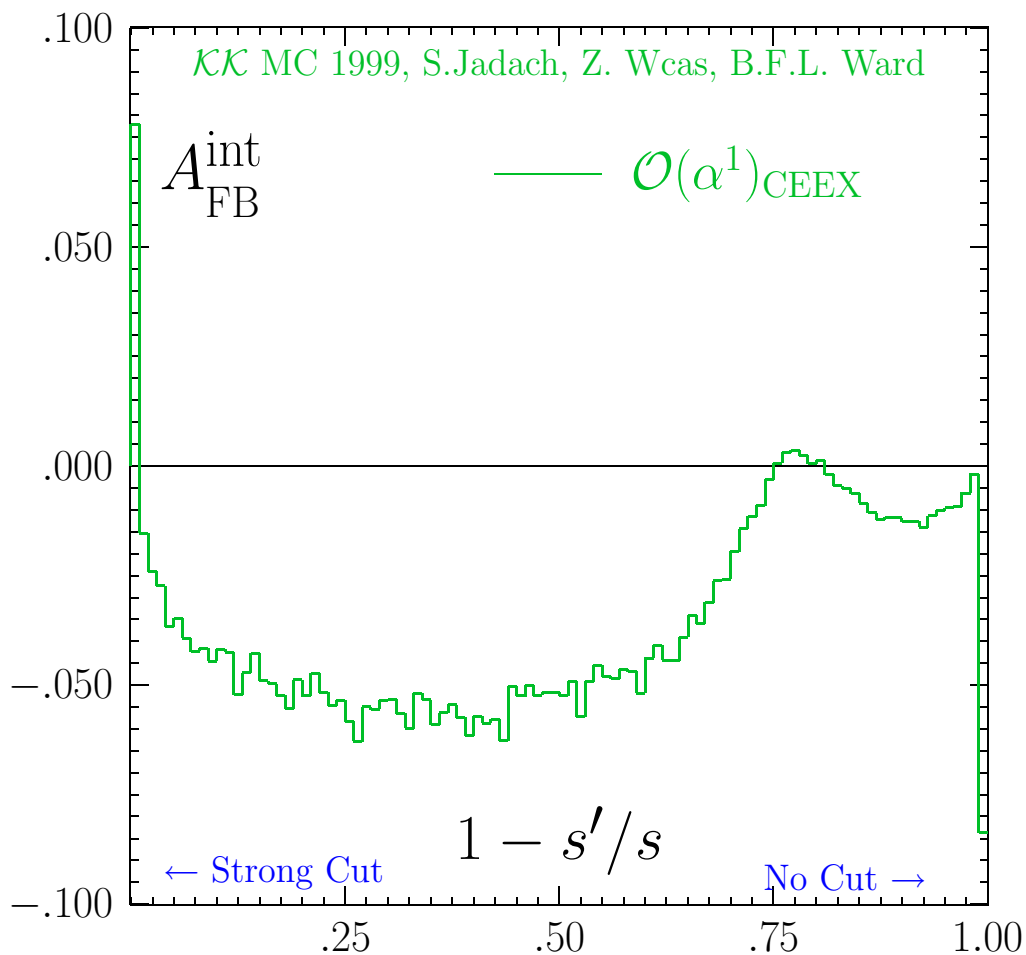
The ISR\*FSR interference correction to  $A_{FB}$  at 189GeV. No cut in  $\cos\theta^*$ . From  $\mathcal{K}\mathcal{K}$  M.C. with  $\mathcal{O}(\alpha^1)_{\text{CEEX}}$  exponentiation at the amplitude level.



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## ISR\*FSR in $A_{FB}$ , energy cut-off study

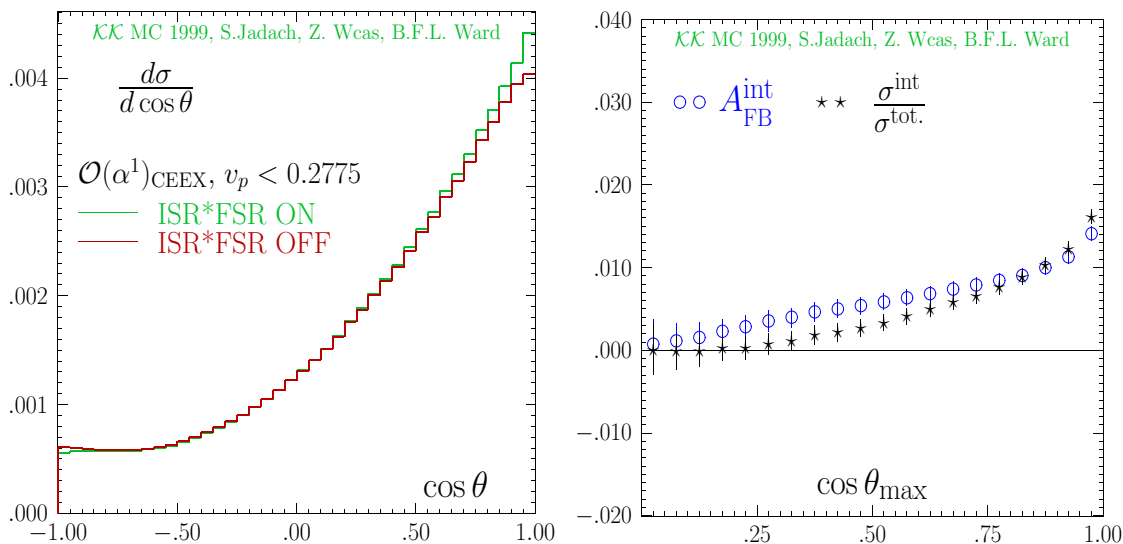
Bin-per-bin  $s'$ -dependence of  $A_{FB}$   
– the ISR\*FSR interference contribution at 189GeV.  
Results from  $\mathcal{K}\mathcal{K}$  M.C. with  $\mathcal{O}(\alpha^1)_{\text{CEEX}}$   
exponentiation at the amplitude level.  
No cut in  $\cos\theta^*$ .



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## ISR\*FSR interf. Realistic acceptance

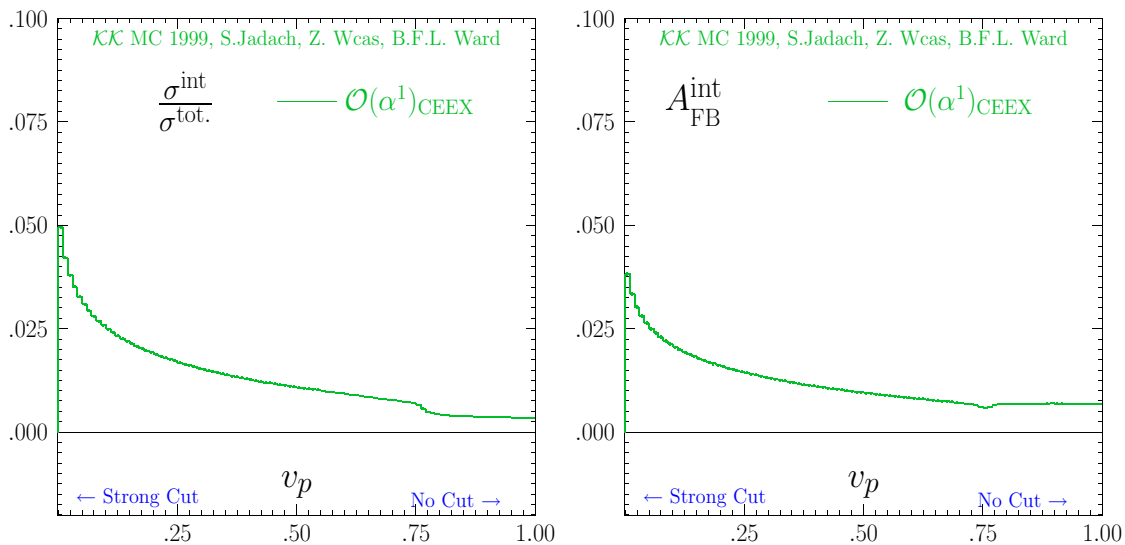
The influence of ISR\*FSR interference at 189GeV.  
 The energy cut is on  $v_p = 1 - Q_{Aleph}^2/s$ , where  
 $Q_{Aleph}^2$  is s-channel propagator variable of ALEPH.  
 The angular cut is  $|\cos \theta| < \cos \theta_{\max}$  Scattering angle  
 is  $\theta = \theta^\bullet$ . [Angle  $\theta^\bullet$  is defined in Phys. Rev. **D41**, 1425 (1990)]



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## ISR\*FSR interf. Realistic acceptance

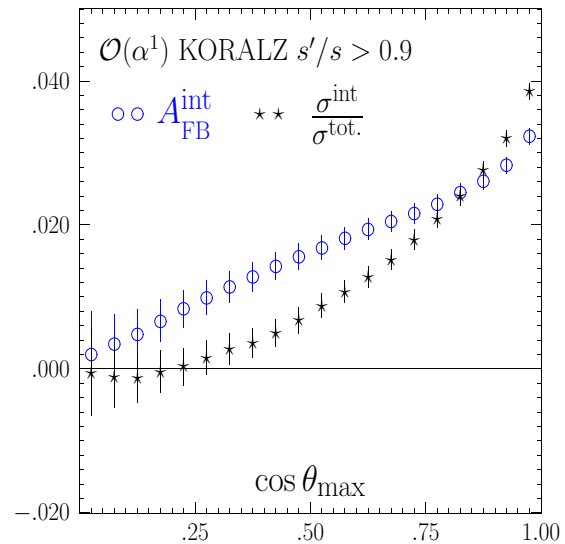
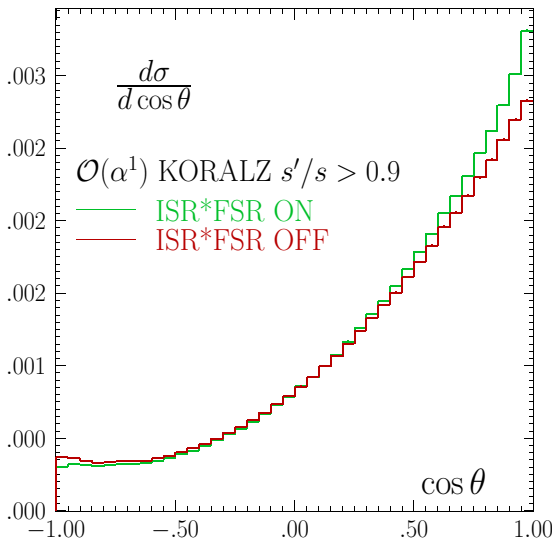
The influence of ISR\*FSR interference at 189GeV.  
The energy cut is on  $v_p = 1 - Q_{Aleph}^2/s$ , where  
 $Q_{Aleph}^2$  is s-channel propagator variable of ALEPH.  
No angular cut.



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## ISR\*FSR interf. KORALZ 1-st order

The influence of ISR\*FSR interference at 189GeV.  
 The energy cut is on  $s'/s$ , where  $s' = m_{f\bar{f}}^2$ . The  
 angular cut is  $|\cos\theta| < \cos\theta_{\max}$  Scattering angle is  
 $\theta = \theta^\bullet$ . [Angle  $\theta^\bullet$  is defined in Phys. Rev. **D41**, 1425 (1990)]



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## Appendix: $\mathcal{K}\mathcal{K}$ versus our older MC's and plans

Feature	KORALB	KORALZ	$\mathcal{K}\mathcal{K}$ now	$\mathcal{K}\mathcal{K}$ 2000
ISR	$\alpha + \alpha L$	$(\alpha + \alpha L + \alpha^2 L^2)_{\text{exp}}$	$(\dots + \alpha^3 L^3)_{\text{exp}}$	$(\dots + \alpha^3 L^3)_{\text{exp}}$
FSR	$\alpha + \alpha L$	$(\alpha + \alpha L + \alpha^2 L^2)_{\text{exp}}$	$(\dots + \alpha^2 L^2)_{\text{exp}}$	$(\dots + \alpha^3 L^3)_{\text{exp}}$
ISR*FSR interf.	$\alpha + \alpha L$	$\alpha + \alpha L$ , no exp.	$(\alpha + \alpha L)_{\text{exp}}$	$(\alpha + \alpha L)_{\text{exp}}$
Exponentiation	NONE	for $ M(p_i) ^2$	for $M(p_i)$	for $M(p_i)$
Exact m.el. for real photons	up to 1	1, 2coll.	1, 2coll, 3coll.	up to 3
El-Weak	No Z-reson.	YES	YES	YES
Beam polar.	long+trans.	longit.	long+trans.	long+trans.
$\tau$ polar.	long+trans.	longit.	long+trans.	long+trans.
Hadronization	—	Yes	Yes	Yes
$\tau$ decay	Yes	Yes	Yes	Yes
Inclusive mode	—	No	Yes	Yes
Beamstrahlung	—	No	Yes	Yes
beam spread	—	No	Yes	Yes
$\nu\nu$ channel	—	Yes	No	Yes
$ee$ channel	—	No	No	Yes
$tt$ channel	—	No	No	???
$WW$ channel	—	No	No	???

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## Conclusions

$\mathcal{K}\mathcal{K}$  Monte Carlo and KORALZ answers on ISR\*FSR Interference:

- For typical exp. energy cut 0.3 ISR\*FSR int. is about 1.5% in  $\sigma_{tot}$  and  $A_{FB}$ .
- For energy cut 0.1 it is twice bigger.
- The cut  $|\cos\theta| < 0.9$  makes it 25% smaller.
- The  $\mathcal{O}(\alpha^1)$  ISR\*FSR int. is under total control using KORALZ and  $\mathcal{K}\mathcal{K}$  Monte Carlo for arbitrary cuts.
- Effects beyond  $\mathcal{O}(\alpha^1)$  are negligible, ( $<20\%$  of  $\mathcal{O}(\alpha^1)$ ), except when energy cut is stronger than 0.1.
- ISR\*FSR int. at Z radiative return is very small, as expected.
- Change from  $s'$  to  $Q^2$ -propagator in energy cut has no effect.