

# NLO corrections in the initial state parton shower Monte Carlo

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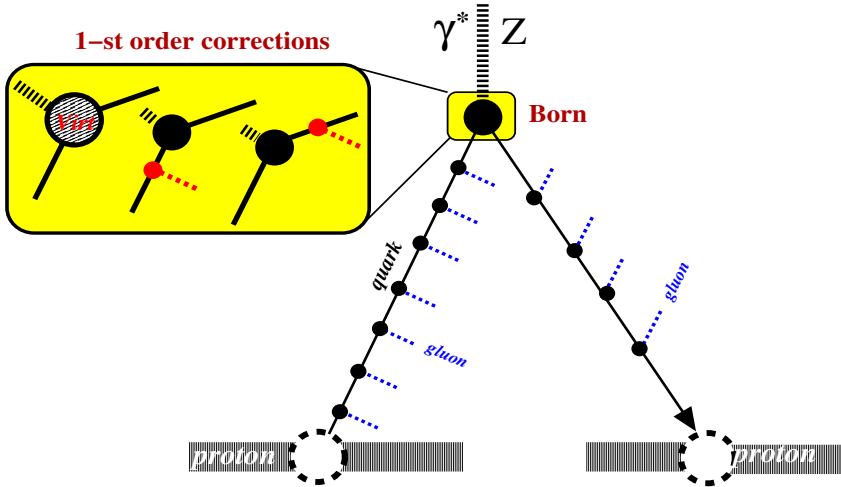
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- ▶ NLO corrections to hard process  
(an alternative to MCatNLO and/or POWHEG)
- ▶ NLO corrections in the ladder  
(for NLO parton shower MC + NNLO hard process)

# NLO correcting HARD process



# The essence of our NLO methodology:



$$\sum_{m=0}^{\infty} \left\{ \left| \begin{array}{c} \vdots \\ \text{[Diagram: Square vertex, gluon lines 1, 2, ..., m]} \\ \vdots \end{array} \right|^2 + \sum_{j=1}^{n-1} \left| \begin{array}{c} \vdots \\ \text{[Diagram: Square vertex, gluon lines 1, 2, ..., n-1, j]} \\ \vdots \end{array} \right|^2 + \sum_{r=1}^m \left| \begin{array}{c} \vdots \\ \text{[Diagram: Square vertex, gluon lines 1, 2, ..., r, m]} \\ \vdots \end{array} \right|^2 \right\}$$

NLO real/virtual distributions (subtracted) from Feynman diags

$$\left| \begin{array}{c} \vdots \\ \text{[Diagram: Square vertex, incoming q, outgoing \gamma^*, gluon g]} \\ \vdots \end{array} \right|^2 = \left| \begin{array}{c} \vdots \\ \text{[Diagram: Circle vertex, incoming q, outgoing \gamma^*, gluon g]} \\ \vdots \end{array} \right|^2 + \left| \begin{array}{c} \vdots \\ \text{[Diagram: Circle vertex, incoming q, outgoing \gamma^*, gluon g]} \\ \vdots \end{array} \right|^2 - \left| \begin{array}{c} \vdots \\ \text{[Diagram: Circle vertex, incoming q, outgoing \gamma^*, gluon g]} \\ \vdots \end{array} \right|^2 - \left| \begin{array}{c} \vdots \\ \text{[Diagram: Circle vertex, incoming q, outgoing \gamma^*, gluon g]} \\ \vdots \end{array} \right|^2$$

free of any double/single collinear/soft singularities.

# MC weight with NLO corrs. to DY hard proc.

NLO correction introduced using simple **positive MC weight**:

$$W_{MC}^{NLO} = 1 + \Delta_{S+V} + \sum_{j \in F} \frac{\tilde{\beta}_1(\hat{s}, \hat{p}_F, \hat{p}_B; a_j, z_{Fj})}{\bar{P}(z_{Fj})} \frac{d\sigma_B(\hat{s}, \hat{\theta})}{d\Omega} + \sum_{j \in B} \frac{\tilde{\beta}_1(\hat{s}, \hat{p}_F, \hat{p}_B; a_j, z_{Bj})}{\bar{P}(z_{Bj})} \frac{d\sigma_B(\hat{s}, \hat{\theta})}{d\Omega},$$

$\bar{P}(z) \equiv \frac{1+z^2}{2}$ . The **IR/Col.-finite real** emission part is

$$\begin{aligned} \tilde{\beta}_1(\hat{p}_F, \hat{p}_B; q_1, q_2, k) = & \left[ \frac{(1-\alpha)^2}{2} \frac{d\sigma_B}{d\Omega_q}(\hat{s}, \theta_{F1}) + \frac{(1-\beta)^2}{2} \frac{d\sigma_B}{d\Omega_q}(\hat{s}, \theta_{B2}) \right] \\ & - \theta_{\alpha > \beta} \frac{1 + (1-\alpha-\beta)^2}{2} \frac{d\sigma_B}{d\Omega_q}(\hat{s}, \hat{\theta}) - \theta_{\alpha < \beta} \frac{1 + (1-\alpha-\beta)^2}{2} \frac{d\sigma_B}{d\Omega_q}(\hat{s}, \hat{\theta}), \end{aligned}$$

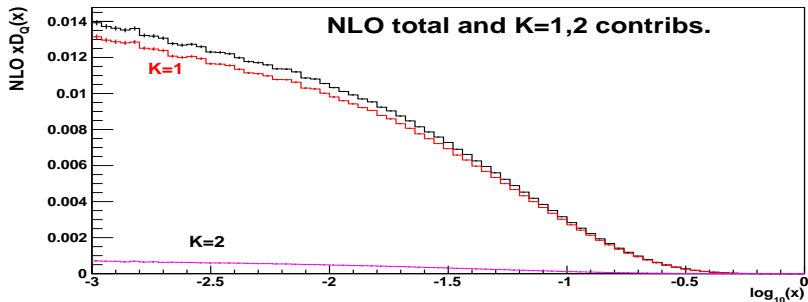
the **kinematics independent virtual+soft** correction is

$$\Delta_{V+S} = \frac{C_F \alpha_s}{\pi} \left( \frac{1}{3} \pi^2 - 4 \right) + \frac{C_F \alpha_s}{\pi} \frac{1}{2}$$

Terms like  $\left( \frac{f(z)}{1-z} \right)_+$  in virt. corrs completely **absent!**

Thanks to transforming MS-bar PDFs to MC Fact scheme,  
(see also Martin+Ryskin 2013)

# Only one single term dominates sum in $W_{MC}^{NLO}$



The (-)NLO contributions from  $K = 1, 2$  single gluons, the one with maximum and another one with next-to-max.  $k_T$ , in the  $x$ -distribution of quark entering  $W$  boson.

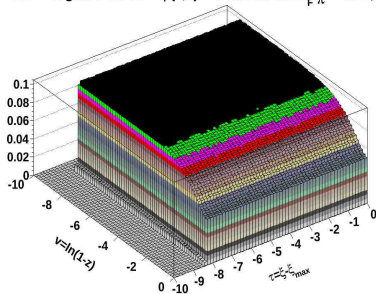
**POWHEG exploits the above. We do it differently, without vetoed/truncated gluons, see next slides...**

# Location and size of the (real) NLO correction on the Sudakov plane (rapidity, $\ln(1-z)$ )



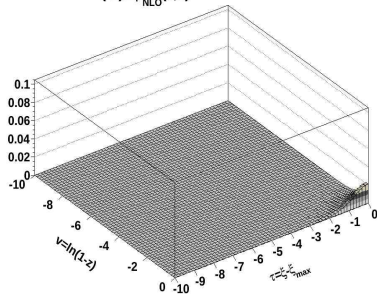
LO inclusive

LO 1-gluon distr.  $\rho(\tau, v)$  Plateau at  $2C_F \frac{\alpha_s}{\pi} = 0.10$ ;



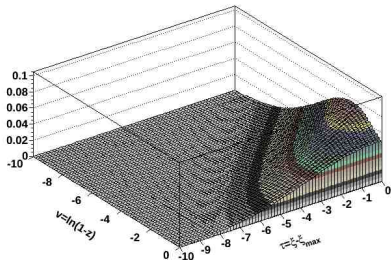
pure NLO

$(-1) \Delta \rho_{\text{NLO}}(\tau, v)$

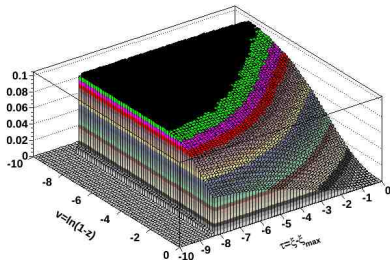


# Glucos generated in angular ordering and re-ordered in kT

LO gluon  $K=1$



LO gluon  $K>1$



Sudakov suppression for the highest kT gluon ( $K=1$ )!

Our NLO weight with summation is ignorant about the above kT (re-)ordering.

The summation (or max. kT-selection) takes care of picking up correctly the hardest gluon, for NLO-completeness.

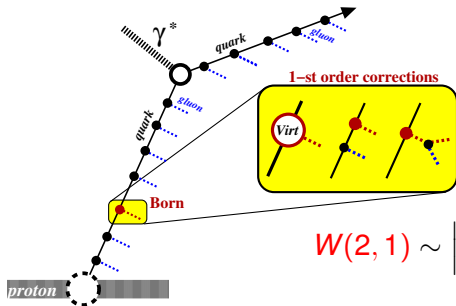
**No need of truncated/vetoed gluon showers.**





# Exclusive NLO-corrections to the middle-of-the-ladder kernels for NLO Monte Carlo parton shower

# NLO-corrected middle-of-the-ladder kernel, $C_F^2$

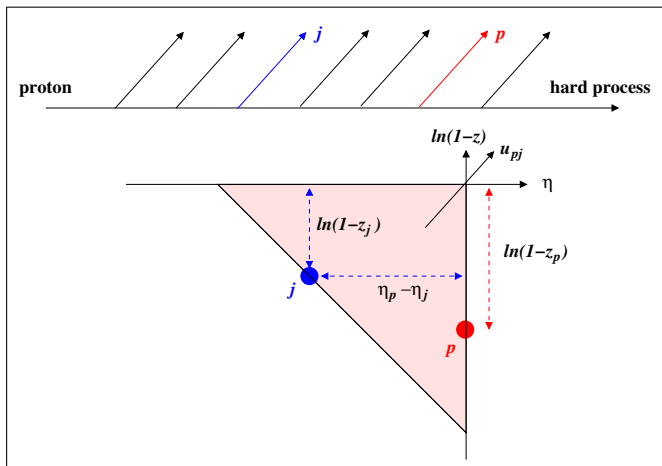


$$W(2,1) \sim \left| \begin{array}{c} 2 \\ | \\ 1 \end{array} \right|^2 = \left| \begin{array}{c} 2 \\ | \\ 1 \end{array} \right|^2 + \left| \begin{array}{c} 2 \\ | \\ 1 \end{array} \right|^2 - \left| \begin{array}{c} 2 \\ | \\ 1 \end{array} \right|^2$$

$$\bar{D}_B^{[1]}(x, Q) = e^{-S_{ISR}} \sum_{n=0}^{\infty} \left\{ \begin{array}{c} x \\ | \\ n \\ | \\ n-1 \\ | \\ \vdots \\ | \\ 2 \\ | \\ 1 \end{array} \right|^2 + \sum_{p=1}^n \begin{array}{c} | \\ | \\ n \\ | \\ n-1 \\ | \\ \vdots \\ | \\ p \\ | \\ \vdots \\ | \\ 2 \\ | \\ 1 \end{array} + \sum_{p=1}^n \sum_{j=1}^{p-1} \begin{array}{c} | \\ | \\ n \\ | \\ p \\ | \\ \vdots \\ | \\ j \\ | \\ \vdots \\ | \\ 1 \end{array} \right\} = e^{-S_{ISR}} \left\{ \delta_{x=1} + \right.$$

$$\left. + \sum_{n=1}^{\infty} \left( \prod_{i=1}^n \int_{Q > a_i > a_{i-1}} d^3 \eta_i \rho_{1B}^{(1)}(k_i) \right) \left[ 1 + \sum_{p=1}^n \beta_0^{(1)}(z_p) + \sum_{p=1}^n \sum_{j=1}^{p-1} W(\tilde{k}_p, \tilde{k}_j) \right] \delta_{x=\prod_{j=1}^n x_j} \right\}.$$

# Define variable $u_{pj}$ for “u-ordering” in the middle of the ladder

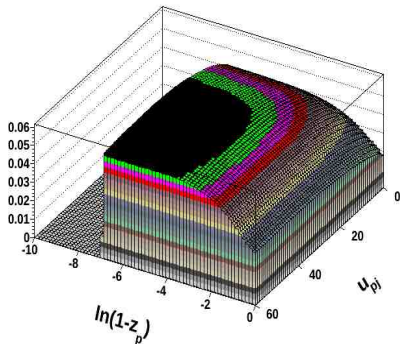


$$u_{pj} = |\eta_p - \eta_j| + \lambda \ln(1 - z_j), \quad \lambda \sim 1 - 2.$$

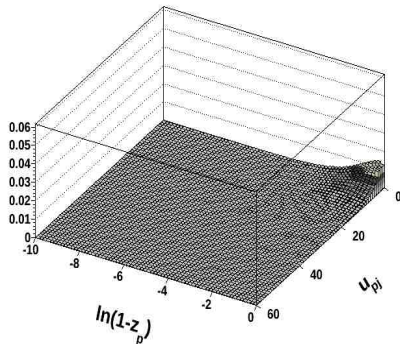
Variable  $\eta$  is rapidity,  $z$  is conventional lightcone variable.

# Location and size of the (real) NLO correction in the ladder on the Sudakov log space

LO, all spect. gluons



pure NLO, all spect. gluons



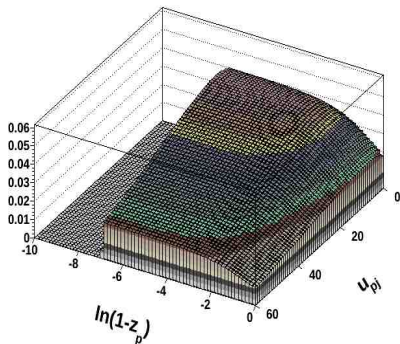
LO inclusive distribution features triple-log IR/coll. singularity, seen as a plateau in 2-dim. projection.

NLO correction IR/coll. finite, nonzero in the corner of the size  $\sim 1$ .

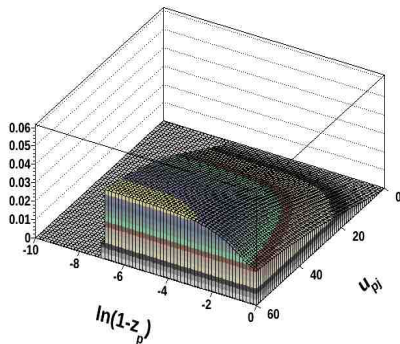
# Split of inclusive LO distribution of gluons into contr. from the u-hardest one and the rest



LO, hardest spect. gluon  $K=1$



LO, spect. gluons  $K>1$

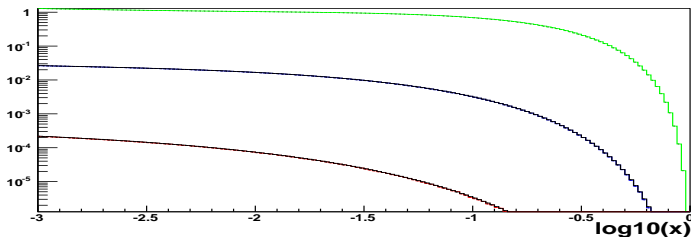


Distribution of the hardest (in  $u_{p_j}$ ) LO spectator gluon approximates well the total distribution in small corner where NLO is non-zero.

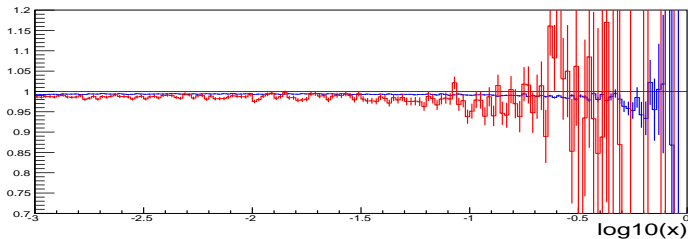
# Repetition of test for NLO-corrected ladder

**OLD:** NLO MC vs. analyt. NLO kernels. Perfect agreement

LO+NLO (green), NLO for 1 (blue) and 2 (red) insertions



Ratios: (1 or 2 insertions)/exact

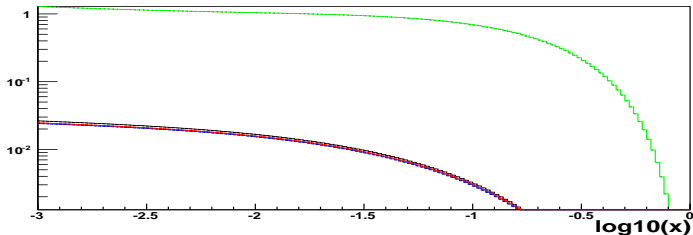


Single ladder, 1GeV-1TeV, 1 or 2 kernels NLO-corrected. (Slow in CPU time).

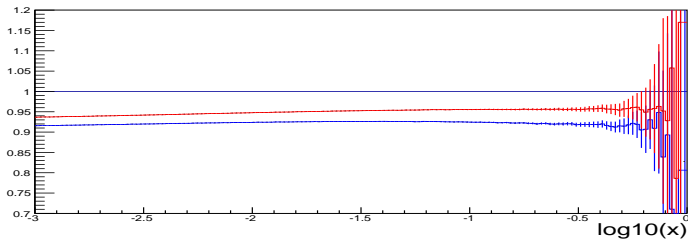
# Repetition of test for NLO-corrected ladder

**NEW:** NLO contrib. to 1 kernel, 1 and 2 gluons with max. kT

LO+NLO (green), one insertions from 1 (blue) or 2 (red) hardest gluons



Ratios: (1 or 2 hardest gluons)/exact



This difference  $\sim 15\%$  is formally the NNLO/NLO class. (Faster in CPU time).

- ▶ **An alternative (to MC@NLO or POWHEG) scenario for NLO-corrected hard proc. and LO PSMC is proposed.**
- ▶ **Parton shower MC implementing complete NLO DGLAP in the ladders in exclusive way is feasible.**
- ▶ Long term: NLO ladder + NNLO hard process, (but LO ladder + NLO hard proc. to be optimized first!)
- ▶ Most likely application: high quality QCD+EW+QED MC with hard process like  $W/Z/H$  boson production.
- ▶ Potential gains from new QCD methods are:
  - reducing uncertainties due to PDFs
  - easier implementation of NLO and NNLO corrections to hard process.  
Due to better treatment of “trivial” (albeit numerically sizeable) soft gluon corrections,
  - better environment for low  $x$  resumm. (BFKL, CCFM),
  - and more...